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Federal State Budgetary Educational
Establishment
of Higher Education
“Ufa University of Science and Technologies”

Strength of materials
department

Course Work

)) Strength calculation in tension, torsion and bending))

Variant № 1

T3D-217b

	Surname and name	Date	Signature
Completed by	Aib-zapemu Bashir	11.12.23	
Checked by			
Accepted by			



USATU

СОВЕТНИЧЕСТВО
МАТЕРИАЛОВ

Computational and graphical work of strength of material

Group

730-2176

Name and surname

Cavusse Alexey Kozhevnikov

Variant

1

Date of issue

25.06.2023

Deadline

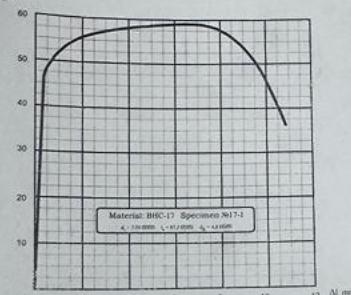
11.06.2023

Lecturer

M. M.

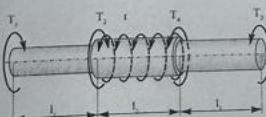
1. Calculation of physical & mechanical properties of materials.

F, kN



Task: according to a given diagram of material tension, it is necessary to determine the basic mechanical characteristics - the limit of proportionality, yield limit, strength limit, tensile stress. Determine the cross-sectional area of the sample before and after the tests, the relative residual elongation, narrowing. Calculate permissible stresses.

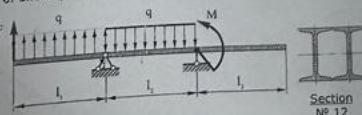
4. Checking calculation of strength of staged rod under torsion.



Task: plot torque moments, shear stresses in fractions of d^{-3} . Perform strength analysis and determine the base rod diameter d . Plot relative and absolute rotation angles, shear stresses and distribution diagram of tangential radial stress in a dangerous section.

t_1, m	t_2, m	t_3, m	T_1, kNm	T_2, kNm	T_3, kNm	T_4, kNm
0,5	0,8	0,5	22	36	31	15
$\frac{t_1}{d}$	$\frac{t_2}{d}$	$\frac{t_3}{d}$	$\frac{T_1}{D_1^3}$	$\frac{T_2}{D_2^3}$	$\frac{T_3}{D_3^3}$	$\frac{T_4}{D_4^3}$
2,6	0,4	3,0	4/4	4/4	4/4	4/4
						Material
						AMuM

6. Cheking calculation of beam made of rolled sections.



Task: to draw plots of internal force factors, stress distribution in a dangerous section with indicating the most loaded points. Check that the strength condition is met. The section is made of standard rolling sections.

Input data for tasks 6 and 7:

l_1, m	l_2, m	l_3, m	F, kN	$q, \text{kN/m}$	M, kNm	Steel brand
0,7	0,6	0,5	43	41	24	Crl5

2. Designing calculation of strength of staged rod.



Task: for a given stepped rod it is necessary to build distribution diagrams of longitudinal forces, plot of stresses in fractions of the area cross-section A. Find the cross-sectional area A according to strength conditions. Plot normal stress. Construction material is taken from task 1.

3. Checking calculation of rod strength and stiffness.



Task: for a rod with a constant cross-sectional area A4, it is necessary to plot the longitudinal forces and axial displacements, perform strength and stiffness calculations.

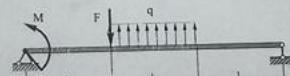
Input data for tasks 2 and 3:

F, kN	l_1, m	l_2, m	l_3, m	t, m
33	0,2	0,4	1,0	
$q, \text{kN/m}$	A_1/A	A_2/A	A_3/A	
14	2,5	1,5	2,7	

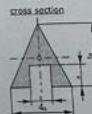
Additional data for task 3:

Material
20X
A_u, cm^2
7,7

5. Designing calculation of strength under bending.

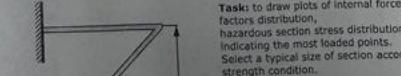


Task: to draw internal force factors distribution diagrams. Match sizes of beam cross section according to strength conditions. Plot dangerous section stress distribution with noticing the most loaded points. Suggest the section position best option.

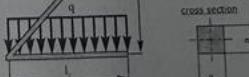


l_1, m	l_2, m	l_3, m	F, kN	$q, \text{kN/m}$	M, kNm	Material
0,2	0,3	0,2	20	5	5	C412-28

7. Designing calculation of strength of plane frame.



Task: to draw plots of internal force factors distribution, hazardous section stress distribution indicating the most loaded points. Select a typical size of section according to strength condition.



Input data for tasks 6 and 7:

l_1, m	l_2, m	l_3, m	F, kN	$q, \text{kN/m}$	M, kNm	Steel brand
0,7	0,6	0,5	43	41	24	Crl5

①. Calculation of physical & mechanical properties of materials.

Task: according to given diagram of material tension, it is necessary to determine the basic mechanical characteristics: the limit of proportionality, yield limit, strength limit tensile stress. Determine the cross-sectional area of the sample before and after the tests; the relative residual elongation narrowing. Calculate permissible stresses.

$$L_0 = 87,3 \text{ mm}$$

$$\Delta L_{0,2} = L_0 \cdot \frac{\epsilon_0}{100} = 0,175 \text{ mm}$$

$$[\sigma] = ? \quad b_0 = 6 \text{ mm} \quad b_0 \text{ lang}$$

$$[\epsilon] = \frac{b_0 \text{ lang}}{n} \cdot \frac{A}{B}$$

for plastic material $\lambda = 1,5 \dots 2,5$

F_y - yield force

$$F_{0,2} = 50 \text{ kN}$$

$$\Delta L_{0,2} = \frac{F_{0,2}}{A_0} \cdot \frac{b_0}{100}$$

$$\epsilon_{0,2} = \frac{F_{0,2}}{A_0}$$

$$\Delta L = 0,175 \text{ mm} \text{ that corresponds to } d_0 = 7,99 \text{ mm}$$

$$\epsilon = 0,2\% \quad A_0 = \frac{\pi \cdot d_0^2}{4}$$

If yield plateau is absent

$\sigma_{0,2}$ - conventional yield limit

we have $\epsilon = 0,2\%$

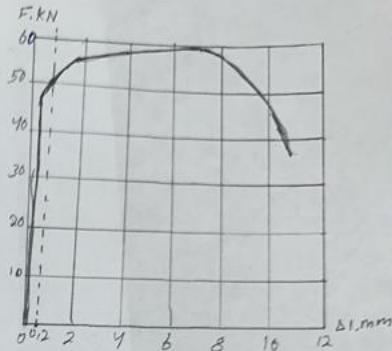
$$\epsilon = \frac{\Delta L}{L_0} \cdot 100 = 0,2$$

$$\Delta L = \frac{\epsilon_0}{100} \cdot L_0 = \Delta L = \frac{0,2}{100} \cdot 87,3 = 1,746 \cdot 10^{-3} = 0,175 \text{ mm}$$

$$A_0 = \frac{\pi \cdot d_0^2}{4} = 50,1^2 \text{ mm}^2$$

$$\sigma_{0,2} = \frac{F_{0,2}}{A_0} = 1017,9 \text{ MPa}$$

$$[\sigma] = \frac{1017,9}{1,5} = 678,6 \text{ MPa} \quad \checkmark$$



Material BHC-17, Specimen No. 71

$$d_0 = 7,99 \text{ mm} \quad l_0 = 87,3 \text{ mm}$$

$$d_k = 4,8 \text{ mm}$$

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C

② Designing calculation of strength of staggered rod

Task: for a given stepped rod it is necessary to build distribution diagrams of longitudinal forces, plot of stresses in fractions of the area cross-section A. Find the cross-sectional area A according to strength conditions. Plot normal stress, construction material is taken from task 1.

① to find N

$$\frac{A_1}{A_0} = 1 \Rightarrow A_1 = 1 \cdot A_0$$

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$$\sum_{x \in \mathcal{C}} f_x = 0$$

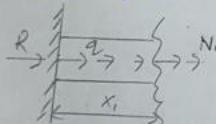
$$+R+2f_5g_1l_1+g_1l_2+g_1l_3=0$$

$$R = -2F - q \cdot l_1 - q \cdot l_2 - q \cdot l_3$$

$$= -2 \cdot 33 - 14 \cdot 0.2 = 14.04 - 14.1$$

$$= 88,4 \text{ kN}$$

2.1 To find N_1 , η



$$\sum F_x = 0$$

$$N_1 + R \cdot q_j \cdot x_1 = 0 \quad N_1 = -R \cdot q_j \cdot x_1$$

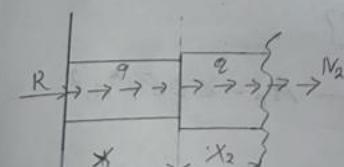
when $x_1 = 0$

$$N_1 = 88,4 - 14 \cdot 0 = 88,4 \text{ kN}$$

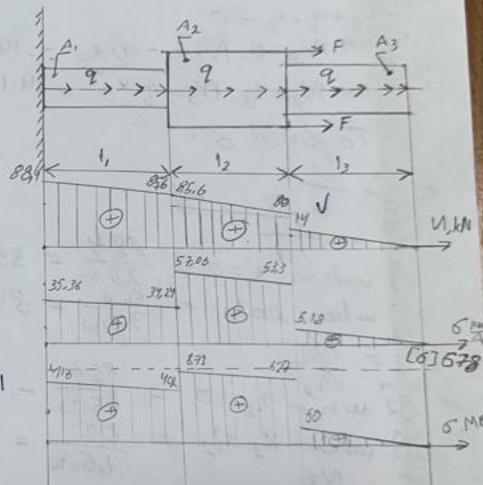
$$N_1 = -\infty, \quad \text{when } x_1 = L$$

$$N_t = 88,4 - 14 \cdot 0,2 = 85,6 \text{ KN}$$

2.2 to find N_2 ?



$$N_2 + R = q \cdot x_1 + q \cdot x_2 = 0 \quad N_2 = -R - q \cdot x_1 - q \cdot x_2$$



Input data for task 2

EKN	$l_{i,m}$	$l_{z,m}$	$l_{y,m}$
33	0.2	0.9	1.0
$q, kNm/m$	A _{1A}	A _{2/A}	A _{3/A}
M	2.5	1.5	2.7

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Checking
Ans

when $x_2 = 0$

$$N_2 = -R - q \cdot l_2 - q \cdot x_2 \\ 88,4 - 14 \cdot 0,2 = 85,6 \text{ kN}$$

when $x_2 = l_2$

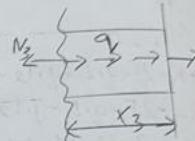
$$N_2 = -R - q \cdot l_1 - q \cdot x_2 = 88,4 - 14 \cdot 0,2 - 14 \cdot 0,4 = 80 \text{ kN}$$

2.3 To find N_3

$$-N_3 + q \cdot x_3 = 0$$

$$\text{when } N_3 = 0 \quad N_3 = -q \cdot x_3 = -14 \cdot 0 = 0$$

$$\text{when } N_3 = l_3 \quad N_3 = q \cdot x_3 = 14 \cdot 1 = 14 \text{ kN}$$



③ To find σ

$$\sigma = \frac{M}{A_0}$$

$$\sigma_1 = \frac{N_1}{A_0}$$

$$\sigma_1 \text{ when } x_1 = 0 = \frac{88,4}{2,5 A_0} = 35,36 \frac{\text{kN}}{A_0}$$

$$\sigma_1 \text{ when } x_1 = l_1 = \frac{85,6}{2,5 A_0} = 34,24 \frac{\text{kN}}{A_0}$$

$$\sigma_2 = \frac{N_2}{A_0}$$

$$\sigma_2 \text{ when } x_2 = 0 = \frac{85,6}{1,5 A_0} = 57,06 \frac{\text{kN}}{A_0}$$

$$\sigma_2 \text{ when } x_2 = l_2 = \frac{80,4}{1,5 A_0} = 53,3 \frac{\text{kN}}{A_0}$$

$$\sigma_3 = \frac{N_3}{A_0}$$

$$\sigma_3 \text{ when } x_3 = 0 = 0 \frac{0}{A_0} = 0 \frac{\text{kN}}{A_0}$$

$$\sigma_3 \text{ when } x_3 = l_3 = \frac{14}{2,7 A_0} = 5,18 \frac{\text{kN}}{A_0}$$

$$\sigma_{\max} \leq [\sigma] = \frac{57,06 \cdot 10^3}{A_0} \leq [\sigma]$$

$$A_0 \geq \frac{157,06 \cdot 10^3}{678,6} \quad A_0 \geq \frac{57,06 \cdot 10^3}{678,6} \quad A_0 = 0,084 \text{ m}^2$$

$$= 84 \text{ mm}$$

let's take $A_0 = 85 \text{ mm}^2$

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checking

$$\frac{\Delta A}{mm^2} = MPa \quad \frac{N}{MPa} = mm^2$$

$$\sigma_1 = \frac{35,36 \cdot 10^3}{85} = 416 \text{ MPa}, \quad \frac{34,24 \cdot 10^3}{85} = 402 \text{ MPa}$$

$$\sigma_2 = \frac{57,06 \cdot 10^3}{85} = 671 \text{ MPa}, \quad \frac{53,31 \cdot 10^3}{85} = 627 \text{ MPa}$$

$$\sigma_3 = \frac{5,18 \cdot 10^3}{85} = 60 \text{ MPa}$$

✓

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(4) Checking calculation of strength of staged rod under torsion

Task: plot torque moments, shear stresses in fractions

of 1/3 per gear strength analysis and determine the least rad. diameter of

Polar relative and absolute rotation angles shear.

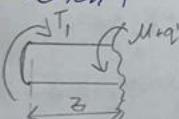
Stresses and distribution diagram of tangential radial stress in a dangerous section.

$$-T_1 - T_2 + t \cdot l_2 + T_4 + T_3 = 0$$

$$T_1 = T_2 + T_3 - t \cdot l_2$$

$$36 - 31 - 22 \cdot 0.8 - 15 = 34.4 \text{ kNm}$$

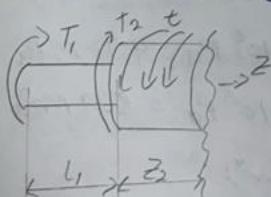
Section 1



$$\sum_{momz} = 0$$

$$-T_1 + M_{q1} = 0$$

$$M_{q1} = \frac{T_1}{2} = 36 \text{ kNm}$$

Section 2 $\sum_{momz} = 0$ 

$$-T_1 - T_2 + t \cdot Z_2 + M_t = 0$$

$$M_{q2} = T_1 + T_2 - t \cdot Z_2$$

$$\text{when } Z_2 = 0$$

$$M_{q2} = T_1 + T_2 - t \cdot Z_2 = -36 + 31 = -67 \text{ kNm}$$

$$\text{when } Z_2 = L_2$$

$$M_{q2} = T_1 + T_2 - t \cdot L_2$$

$$36 + 31 - 22 \cdot 0.8 = 49.4 \text{ kNm}$$

Section 3



$$\sum m_{qs} = 0$$

$$M_{qs} = T_3 = 15 \text{ kN.m}$$

Strength calculations

$$T_{max} \leq [T] \quad T_{max} = 12,67$$

$$[T] = \frac{67}{2} = \frac{G}{D_2} = \frac{G}{4} = \frac{60}{4} = 15$$

$$T_{max} = \frac{M_{qs}}{W_{pl}} = \frac{36}{3,45d} = 10,43 \frac{\text{kN}}{d^3}$$

$$T_{max} = \frac{67}{5,29d^3} = 12,67 \frac{\text{kN}}{d^3}$$

$$T_{max} = \frac{49,9}{5,29d^3} = 9,43 \frac{\text{kN}}{d^3}$$

$$T_{max} = \frac{15}{1,82d^3} = 8,24 \frac{\text{kN}}{d^3}$$

Strength condition

$$\frac{12,67 \text{ kN.m}}{d^3} \leq 15 \text{ MPa} \quad d \geq \sqrt[3]{\frac{12,67 \cdot 10^3}{15 \cdot 10^6}}$$

$\geq 0,095 \text{ m} \geq 95 \text{ mm}$ Let's take $d = 100 \text{ mm}$?

Checking:

$$\frac{9,13 \text{ kNm}}{d^3} = \frac{9,43 \cdot 10^3}{0,1^3} = 9,43 \cdot 10^6 \text{ Pa} = 9,43 \text{ MPa}$$

$$\frac{8,24 \text{ kNm}}{d^3} = \frac{8,24 \cdot 10^3}{0,1^3} = 8,24 \cdot 10^6 \text{ Pa} = 8,24 \text{ MPa}$$

$$\Theta_2^{22=0} = \frac{J_{qs}}{G \cdot I_{pq}} = \frac{I_{pq} \cdot \pi D^4}{32} (1 - \alpha^4)$$

$$\Theta_2^{22=0} = \frac{67 \cdot 10^3}{27 \cdot 10^9 \cdot 0,000794989} = 0,001214 \text{ rad/m} = 3,12 \text{ rad/m}$$

$$G = 27 \text{ GPa} \quad I_{pq} = \frac{\pi (2,601)}{32} (1 - 0,15^4) = 4,48 \cdot 10^{-4} \text{ m}^4$$

$$\alpha_2 = \frac{32 \cdot d_2}{\theta} = \frac{0,4}{3,0} = 2,8 \cdot 10^{-3} \text{ rad/m} = 2,98 \text{ rad/m}$$

⑥ Checking calculation of beam made of rolled sections

Task: to draw plots of internal force factors of stress distribution in a dangerous section with indicating the most loaded points
Check that the section is made of standard rolling sections

$$\sum F_y = 0 \quad + X_A = 0 \quad \checkmark$$

$$F + q \cdot l_1 + Y_A - q \cdot l_2 + Y_B \\ + M = 0$$

$$\sum F_y = 0 + q \cdot l_1 - q \cdot l_2 + f \\ + Y_A + Y_B$$

$$\sum m_{mom A} = 0$$

$$-F \cdot l_1 - R \cdot q \cdot l_1 \frac{l_1}{2} + q \cdot l_2 \\ - \frac{l_2^2}{2} + Y_B \cdot l_2 + M = 0$$

$$Y_B = F \cdot l_1 + q \cdot l_1 \cdot \frac{l_1}{2} + q \cdot l_2 \cdot \frac{l_2}{2} - M \\ - l_2 \cdot$$

$$Y_B = 43 \cdot 0.7 + 41 \cdot 0.7 \cdot \frac{0.7}{2} + 41 \cdot 0.6 \cdot \frac{0.6}{2} - 24 \\ = 39,208 \text{ KN} \quad \checkmark$$

$$\sum m_{mom B} = 0$$

$$-F(l_1 + l_2) - q \cdot l_1 \left(\frac{l_1}{2} + l_2 \right) - Y_A \cdot l_2 \\ + q \cdot l_2 \cdot \frac{l_2}{2} + M = 0$$

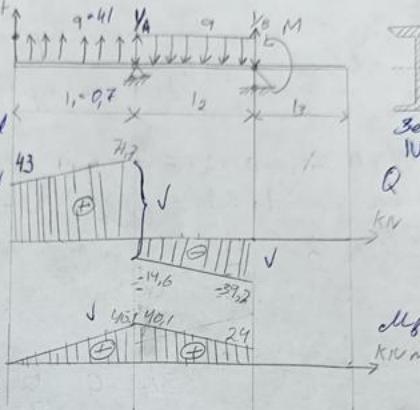
$$Y_A = -F(l_1 + l_2) - R \cdot l_1 \left(\frac{l_1}{2} + l_2 \right) + R \cdot l_2 \cdot \frac{l_2}{2} + M$$

$$Y_A = -43(0.7 + 0.6) - 41 \cdot 0.7 \left(\frac{0.7}{2} + 0.6 \right) + 43 \cdot 0.6 \cdot \frac{0.6}{2} + 24 = -863 \text{ kN}$$

Checking

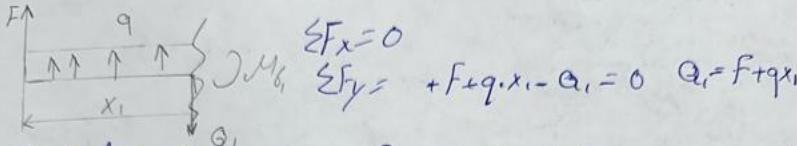
$$q \cdot l_1 - q \cdot l_2 + f + Y_A + Y_B = 0$$

$$41 \cdot 0.7 - 41 \cdot 0.6 + 43 + 39,2 + (-863) = 0$$



l ₁ M	l ₂ M	l ₃ A	Filling	Mid. M. kNm	Steel. b. mm
0.7	0.6	0.5	43	24	C75

Section

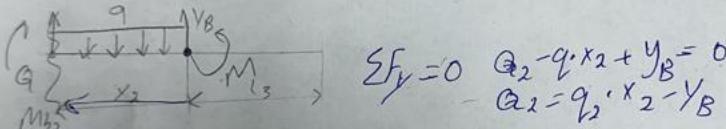


$$\sum M_b = 0 \quad \sum F_x = 0 \quad +F + q \cdot x_1 - Q_1 = 0 \quad Q_1 = F + q \cdot x_1$$

Q1. when $Q_1 = 0$ $Q_1 = F + q \cdot x_1 \quad q_3 + q_1 \cdot 0 = 43 \text{ kN} \quad \checkmark$

Q2. when $x_1 = L$, $Q_1 = F + q \cdot x_1 \quad q_3 + q_1 \cdot 0.7 = 71.7 \text{ kN} \quad \checkmark$

Section 2



$$\sum F_y = 0 \quad Q_2 - q \cdot x_2 + Y_B = 0 \quad Q_2 = q \cdot x_2 - Y_B$$

Q2. when $x_2 = 0 \quad q \cdot x_2 - Y_B \quad 41.0 - 39,208 = -39,208 \text{ kN}$

Q2. when $x_2 = L \quad q \cdot x_2 - Y_B \quad 41.0 \cdot 0.6 - 39,208 = -14,60 \text{ kN}$

$$M_{b1} = f \cdot F \cdot x_1 + q \cdot x_1 \cdot \frac{x_1}{2} \quad M_{b1}(x_1=0) = 0 \\ M_{b1} (x_1=L) \quad f \cdot L_1 + \frac{q_1 L^2}{2} \quad 43 \cdot 0.7 + \frac{41.0 \cdot 0.7^2}{2} = 40,145$$

$$\sum mom_x = 0 \quad -M_{b2} - q \cdot x_2 \cdot \frac{x_2}{2} + Y_B \cdot x_2 + M = 0$$

$$M_{b2} = -q \cdot L_2 \cdot \frac{L_2}{2} + Y_B \cdot L_2 + M$$

$$M_{b2} (x_1=0) \quad M_{b2} = M = 24 \text{ kNm}$$

$$M_{b2} (x_2=L) \quad M_{b2} = -q \cdot L_2 \cdot \frac{L_2}{2} + Y_B \cdot L_2 + M$$

$$-41.0 \cdot 0.6 \cdot \frac{0.6}{2} + 39,208 \cdot 0.6 + 24 \\ = 40,195 \text{ kNm}$$

$$\sigma_{max} = \frac{\sigma_b \text{ max}}{E} = \frac{w_b \text{ max}}{I_{xx} x_1} = \frac{40,145 \cdot 10^3}{58,4 \cdot 10^{-5}} = 343 \text{ MPa}$$

$\left[\frac{\sigma}{E} \right] = \frac{255 \text{ MPa}}{2} = 127.5 \text{ MPa}$
According to σ_{max} , $\left[\frac{\sigma}{E} \right]$ it will not be able to carry the load
so it's will break.